

Class - 7

Ch - 8

ex 9.1

Date:

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① Express the following as ratios

a) 6 Kg to 10 Kg

$$= \frac{6}{10}$$

$$= \frac{3}{5}$$

$$= 3:5$$

② ₹ 7000 to ₹ 3500

$$= \frac{7000}{3500}$$

$$= \frac{2}{1} = 2:1$$

③ 50 km to 70 km

$$= \frac{50}{70}$$

$$= \frac{5}{7} = 5:7$$

④ Express the following as ratios in the simplest form

a) ₹ 7 and 50 paise to ₹ 4

$$= \frac{7.50}{4}$$

$$= \frac{7.50 \times 100}{4 \times 100}$$

$$= \frac{750}{400}$$

$$= \frac{75}{40}$$

$$= \frac{15}{8}$$

$$= 15:8$$

b) 700 ml to 1 litre

$$= \frac{700}{1}$$

$$= \frac{700}{1 \times 1000}$$

$$= \frac{700}{1000}$$

$$= \frac{7}{10}$$

$$= 7:10$$

$$\boxed{1 \text{ l} = 1000 \text{ ml}}$$

Q1 In a farm house, There are 80 cows and 30 buffaloes. What is the ratio of the cows to the buffaloes?

Soln Total no of cows = 80
Total no of buffaloes = 30

$$\begin{aligned} \text{Ratio} &= \frac{\text{no of cows}}{\text{no of buffaloes}} \\ &= \frac{80}{30} \\ &= \frac{8}{3} \\ &= 8:3 \end{aligned}$$

\therefore The required ratio = 8:3

Q2 In a packet of sweets, for every 20 sweets, there were 4 chocolate bars and the remaining were Toffees. What is the ratio of the Toffees to the chocolates?

Soln Total no of sweets = 20
Total no of chocolate bar = 4
Total no of Toffees = 20 - 4
= 16.

$$\begin{aligned} \text{Ratio} &= \frac{\text{no of Toffees}}{\text{no of chocolates}} \\ &= \frac{16}{4} \\ &= \frac{4}{1} \\ &= 4:1 \end{aligned}$$

\therefore The required ratio = 4:1

- 3 The measure of two angles are in the ratio 7:8 and they are supplementary angles. What are the measures in degree?

Soln

Let the two angles be $7x$ and $8x$
 Since they are supplementary angles
 The sum of the two angles is 180°

$$\Rightarrow 7x + 8x = 180^\circ$$

$$\Rightarrow 15x = 180^\circ$$

$$\Rightarrow x = \frac{180}{15} = 12$$

$$\Rightarrow x = 12$$

$$\begin{array}{r} 12 \\ 15 \overline{) 180} \\ \underline{15} \\ 30 \\ \underline{30} \\ 0 \end{array}$$

$$\therefore \begin{aligned} \text{1st angle} &= 7 \times 12 = 84^\circ \\ \text{2nd angle} &= 8 \times 12 = 96^\circ \end{aligned}$$

1
84
+ 96
<hr/> 180

- 4 The sides of the rectangular field are in the ratio ~~9:7~~ 9:7 and the perimeter is 144 m. Find the sides.

Soln

Let length 'l' be $9x$
 and breadth 'b' be $7x$

perimeter of a rectangle = $2(l+b)$
--

$$\text{Perimeter of the field} = 144 \text{ m}$$

$$\Rightarrow 2(l+b) = 144$$

$$\Rightarrow 2(9x+7x) = 144$$

$$\Rightarrow 2 \times 16x = 144$$

$$\Rightarrow 32x = 144$$

$$\Rightarrow x = \frac{144}{32}$$

$$\Rightarrow x = 4.5$$

$$\therefore \begin{aligned} \text{length} &= 9x \\ &= 9 \times 4.5 \\ &= 40.5 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{breadth} &= 7x \\ &= 7 \times 4.5 \\ &= 31.5 \text{ m} \end{aligned}$$

6 The sides of a triangle are in ratio 2:3:4 and its perimeter is 63 cm. What are the lengths of its sides?

Soln

Let the sides of the Δ be $2x$, $3x$ & $4x$
Perimeter of $\Delta = 63$ cm.

$$\Rightarrow 2x + 3x + 4x = 63$$

$$\Rightarrow 9x = 63$$

$$\Rightarrow x = \frac{63}{9}$$

$$\therefore x = 7$$

\therefore Sides of the Δ

$$= 2x$$

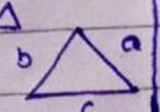
$$= 2 \times 7 = 14 \text{ cm}$$

$$3x$$

$$= 3 \times 7 = 21$$

$$4x$$

$$= 4 \times 7 = 28$$

Perimeter of Δ
 $= a + b + c$


7 Amar divided his collection of stamps in the ratio 6:5 between his two sisters Sheila and Amina. If Sheila received 23 more stamps than Amina, how many stamps did he distribute?

Soln

Let Sheila's share be $6x$

and Amina's share be $5x$

Sheila received 23 more stamps than Amina.

A/O

$$6x - 5x = 23$$

$$\therefore x = 23$$

$$\text{Distribution} = 23 \times (6 + 5)$$

$$= 23 \times 11$$

$$= 253 \text{ stamps.}$$

3 The numerator and denominator of a fraction are in ratio 3:2. If 3 is added to the numerator and 2 is ~~added~~ subtracted from the denominator, a new fraction is formed whose value is $\frac{9}{4}$. Find the original fraction.

Soln

Let the numerator be $3x$
and denominator be $2x$

A/Q

$$\Rightarrow \frac{3x+3}{2x-2} = \frac{9}{4}$$

$$\Rightarrow 4(3x+3) = 9(2x-2) \quad (\text{Cross multiplication})$$

$$\Rightarrow 12x+12 = 18x-18$$

$$\Rightarrow 12+18 = 18x-12x \quad (\text{Like terms})$$

$$\Rightarrow 30 = 6x$$

$$\Rightarrow \frac{30}{6} = x$$

$$\Rightarrow 5 = x$$

$$\therefore x = 5$$

Now,

$$\text{Numerator} = 3x$$

$$= 3 \times 5$$

$$= 15$$

$$\text{Denominator} = 2x$$

$$= 2 \times 5$$

$$= 10$$

9 Alka and Swetha invested ₹1800 and ₹2400 respectively in a small business. They made a profit of ₹1400. They decided to divide the profit between them in the ratio of their investment. How much did each get as profit?

Soln

$$\text{Alka investment} = ₹1800$$

$$\text{Swetha investment} = ₹2400$$

$$\text{Ratio} = \frac{\text{Alka investment}}{\text{Swetha investment}}$$

$$= \frac{3}{4}$$

$$= \frac{3}{4}$$

$$\therefore \text{ratio} = 3:4$$

$$\text{Profit They made} = ₹1400$$

$$\therefore 3x + 4x = 1400$$

$$\Rightarrow 7x = 1400$$

$$\Rightarrow x = \frac{1400}{7}$$

$$\therefore x = 200$$

$$\text{Alka's share} = 3x$$

$$= 3 \times 200$$

$$= ₹600$$

$$\text{Swetha share} = 4x$$

$$= 4 \times 200$$

$$= ₹800$$

10 Two numbers are in the ratio 7:10. If the larger number is 140, what is the smaller number?

Soln Let the smaller no be $7x$
and larger no be $10x$

A/O

$$\text{larger no} = 140$$

$$\Rightarrow 10x = 140$$

$$\Rightarrow x = \frac{140}{10}$$

$$x = 14$$

$$\text{Smaller no} = 7x$$

$$= 7 \times 14$$

$$= 98$$

12 The angles of a pentagon are in the ratio 2:4:2:1:1. If the total measure of the angles of a pentagon is 540° , what are the measures of each angle?

Soln Let the angles of the pentagon be $2x, 4x, 2x, 1x$ and $1x$

$$\text{Total measure of the angles} = 540^\circ$$

$$\therefore 2x + 4x + 2x + 1x + 1x = 540$$

$$\Rightarrow 10x = 540$$

$$\Rightarrow x = \frac{540}{10}$$

$$\therefore x = 54$$

Measure of each angle

$$1^{\text{st}} \text{ angle} = 2x$$

$$= 2 \times 54$$

$$= 108^\circ$$

$$2^{\text{nd}} \text{ angle} = 4x$$

$$= 4 \times 54$$

$$= 216^\circ$$

\therefore The angles are $108^\circ, 216^\circ, 108^\circ, 54^\circ, 54^\circ$

ex 8.3

Q1 Are the two ratios 30:50 and 50:75 equivalent?

$$\Rightarrow \frac{30}{50} = \frac{50}{75}$$

By cross multiplication

$$\Rightarrow 30 \times 75 = 2250$$

$$50 \times 50 = 2500$$

Since $30 \times 75 \neq 50 \times 50$

The ratios are not equivalent.

* Two ratios are said to be equivalent if their corresponding fractions are equivalent.

Q3 Rohit covered 120m in 20 seconds, Then in how much time would he cover 210m?

Sol	Distance covered	Time Taken.
	120 m	20
	210 m	x

$$= 120 : 210 :: 20 : x$$

Product of extremes = Product of means

$$\Rightarrow 120 \times x = 210 \times 20$$

$$\Rightarrow 120x = 4200$$

$$\Rightarrow x = \frac{4200}{120}$$

$$\Rightarrow x = 35$$

$$\begin{array}{r} 35 \\ 12 \overline{) 420} \\ \underline{36} \\ 60 \\ \underline{60} \\ 0 \end{array}$$

\therefore Time taken to cover 210m = 35 seconds.

5 A box of apples cost ₹ 354. How many boxes of can be bought with ₹ 1770

Soln cost of apples No of boxes

354

1

1770

354

x

$$354 : 1770 :: 1 : x$$

Product of extreme = Product of means

$$\Rightarrow \frac{354}{345} x = 1770 \times 1$$

$$\Rightarrow \frac{354}{345} x = 1770$$

$$\Rightarrow x = \frac{1770 \times 345}{354}$$

$$x = 5$$

∴ No of boxes = 5 boxes.

6 The scale of a particular map is 1:1,00,000. on the map, The school is shown 2.5 cm away from Jatin's house. How far is his house from the school? Express this answer in Km.

Soln The scale of map is 1:100000
map distance from house to school = 2.5 cm.

$$\text{original distance} = 2.5 \times 100000 \text{ cm}$$

$$= 250000 \text{ cm}$$

We know that 1 Km = 100000 cm

$$\therefore \frac{250000}{100000} \text{ Km}$$

$$= 2.5 \text{ Km.}$$

∴ The house of Jatin is 2.5 km far away from the school.

7 23 people has lunch in a hotel and the rate per lunch is the same for all. If it cost ₹ 3105 in total, how much will it cost for 60 people to have lunch in the same hotel at the same rate.

<u>Soln</u>	No of people	Cost of the lunch
	23	3105
	60	x

$$= 23 : 60 : 3105 : x$$

Product of extreme = product of mean

$$\Rightarrow 23 \times x = 60 \times 3105$$

$$\Rightarrow 23x = 1,86,300$$

$$\Rightarrow x = \frac{1,86,300}{23}$$

$$\Rightarrow x = ₹ 8100$$

\therefore cost for 60 people to have lunch = ₹ 8100

* $a : b : c : d$

product of extreme = $a \times d$
 product of mean = $b \times c$

8.4

1 125 g of yoghurt provide 4.5 g protein. How many grams of proteins does 100g of yoghurt provide?

Soln 125 g yoghurt provides 4.5 g protein

1g of yoghurt will provide $\frac{4.5}{125}$ g protein

$$\begin{aligned} \therefore 100 \text{ g yoghurt will provide} \\ &= 100 \times \frac{4.5}{125} \text{ g} \\ &= 3.6 \text{ g.} \end{aligned}$$

Q2 In a poultry farm, every 100 birds provide an average of 72 eggs. How many birds will produce 324 eggs?

Soln 100 birds provides an average of 72 eggs

$$\begin{aligned} \text{Average birds for an egg} \\ &= \frac{100}{72} \end{aligned}$$

$$= \frac{25}{18} \text{ birds}$$

$$\begin{aligned} \text{For 324 eggs} \\ &= \frac{25}{18} \times 324 \end{aligned}$$

$$= 25 \times 18$$

$$= 450 \text{ birds}$$

4 50 people consume an average of 110 kg of rice in a week. If 20 more people join the group, how many kilograms of rice will be needed for a week?

Soln 50 people consume 110 kg of rice.
1 man can consume an average of
rice = $\frac{110}{50}$ kg

$$= \frac{11}{5} \text{ kg}$$

If 20 more people join the group
Total no of people = 50 + 20
= 70 people

Rice needed for 70 people for a week
= $\frac{11}{5} \times 70$
= 11 × 14
= 154 kg.

7 In 3 hours, a train covers 195 km. Travelling at the same speed, what distance would the train cover in 5 hours.

Soln Distance covered in 3 hours = 195 km.
Distance covered in 1 hour = $\frac{195}{3}$ km
= 65 km

Distance covered in 5 hours
= 65 × 5
= ~~30~~ 325 km.

Exercise 10.1

①

1. Identify the following pairs of angles as complementary, supplementary or equal.

- (a) 77° and 103° — Supplementary angles
(b) 177° and 177° — Equal angles
(c) 7° and 173° — Supplementary angles
(d) 3° and 87° — complementary angles
(e) 45° and 45° — complementary angles
(f) 90° and 90° — Equal angles.

2. Write the complements of the following angles

- (a) $45^\circ = 90^\circ - 45^\circ = 45^\circ$
(b) $40^\circ = 90^\circ - 40^\circ = 50^\circ$
(c) $10^\circ = 90^\circ - 10^\circ = 80^\circ$
(d) $54^\circ = 90^\circ - 54^\circ = 36^\circ$
(e) $61^\circ = 90^\circ - 61^\circ = 29^\circ$
(f) $36^\circ = 90^\circ - 36^\circ = 54^\circ$
(g) $17^\circ = 90^\circ - 17^\circ = 73^\circ$
(h) $4^\circ = 90^\circ - 4^\circ = 86^\circ$

3. write the supplements of the following angles.

$$(a) 80^\circ = 180^\circ - 80^\circ = 100^\circ$$

$$(b) 10^\circ = 180^\circ - 10^\circ = \del{170} 170^\circ$$

$$(c) 125^\circ = 180^\circ - 125^\circ = 55^\circ$$

$$(d) 138^\circ = 180^\circ - 138^\circ = 42^\circ$$

$$(e) 38^\circ = 180^\circ - 38^\circ = 142^\circ$$

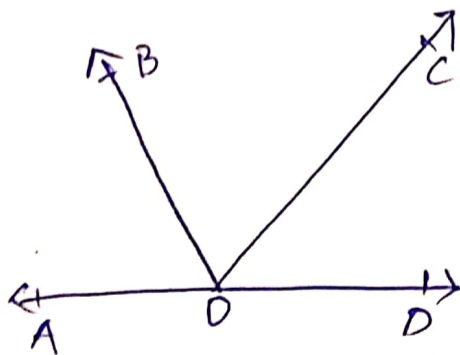
$$(f) 114^\circ = 180^\circ - 114^\circ = 66^\circ$$

$$(g) 100^\circ = 180^\circ - 100^\circ = 80^\circ$$

$$(h) 21^\circ = 180^\circ - 21^\circ = 159^\circ$$

4) Name the following angles in the following

(a)



Ans

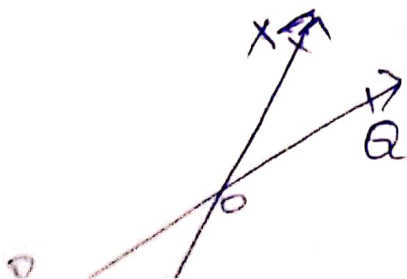
$\angle AOB$ and $\angle COB$

$\angle AOB$ and $\angle DOB$

$\angle BOC$ and $\angle DOC$

$\angle AOC$ and $\angle DOC$

(b)



$\angle POY$ and $\angle QOY$

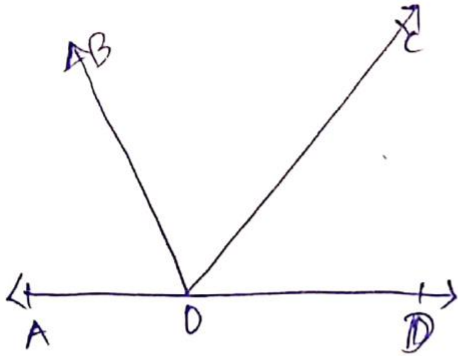
$\angle POY$ and $\angle XOP$

$\angle XOQ$ and $\angle YOP$

$\angle POX$

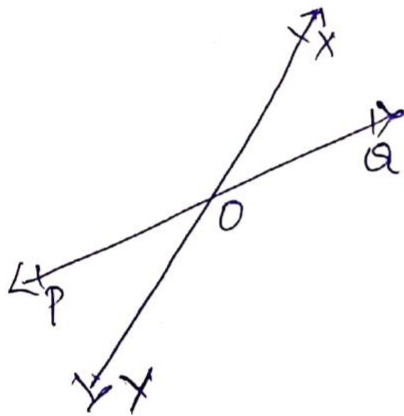
Q 5) Identify the linear pairs of in the fig. in (Q4) above.

(a)



- $\angle AOB$ and $\angle BOC$ are linear pairs
- $\angle AOC$ and $\angle COD$ are linear pairs

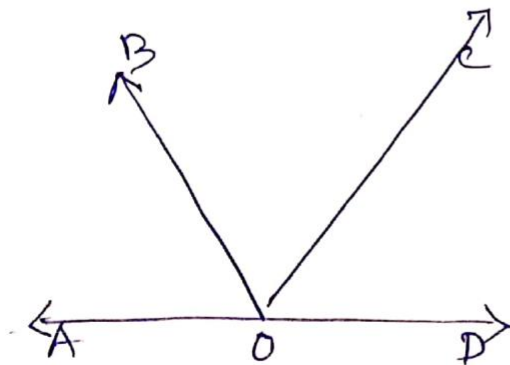
(b)



- $\angle POY$ and $\angle QOX$ are linear pairs
- $\angle POX$ and $\angle QOY$ are linear pairs

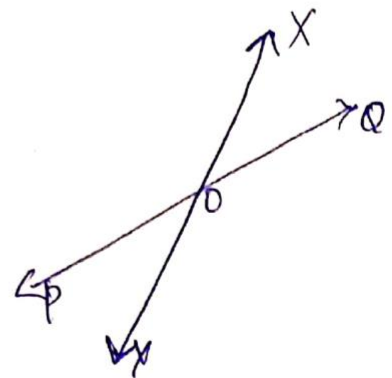
b) Identify the vertically opposite angles in the fig (Q4) above.

a)



$\angle AOB$ and $\angle COD$
are opposite angles

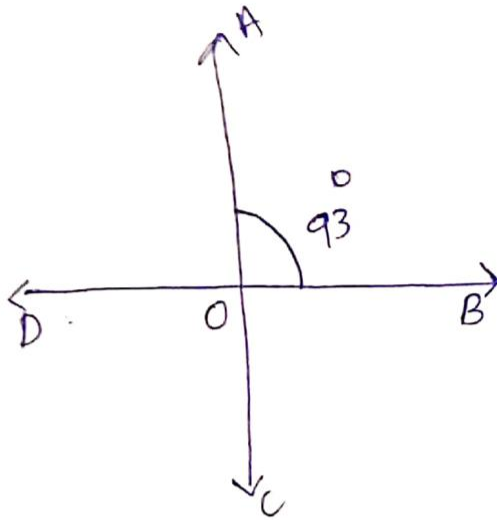
(b)



$\angle POY$ and $\angle QOX$
 $\angle QOY$ and $\angle POX$
no vertically opposite angle

∴ The measure of one angle is given in the following figure. Find all the other angles.

(a)



$$\angle AOB + \angle DOA = 180$$

$$\angle DOA = 180 - \angle AOB = 180 - 93 = \underline{87}^{\circ}$$

$$\angle AOB = \angle COD \quad (\text{opposite angles are equal})$$

then $\angle COD = \underline{93}^{\circ}$

$$\angle BOC = \angle DOA \quad (\text{opposite angles are equal})$$

$$\angle DOA = 87^{\circ}$$

$$\angle BOC = \underline{87}^{\circ}$$

$$\angle AOB = 93^{\circ}$$

$$\angle DOA = 87^{\circ}$$

$$\angle COD = 93^{\circ}$$

$$\angle BOC = 87^{\circ}$$



$$\angle POS + \angle ROS = 180^\circ \quad (\text{Linear pair})$$

$$\angle ROS = 180^\circ - \angle POS$$

$$= 180^\circ - 13^\circ = \underline{\underline{167^\circ}}$$

$$\angle POS = \angle ROQ \quad (\text{Vertically opposite angles are equal})$$

$$\angle ROQ = 13^\circ$$

$$\angle ROS = \angle QOP = 167^\circ \quad (\text{Vertically opposite angles are equal})$$

$$\angle POS = 13^\circ$$

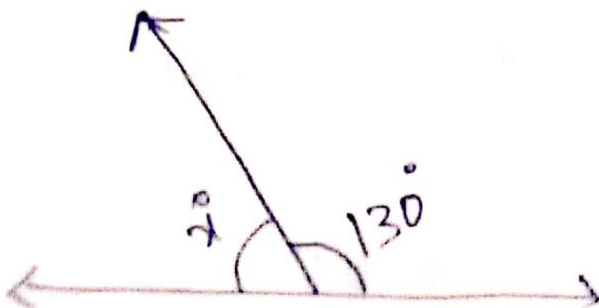
$$\angle ROS = 167^\circ$$

$$\angle ROQ = 13^\circ$$

$$\angle QOP = 167^\circ$$

Find the measure of x in the following figure

(a)

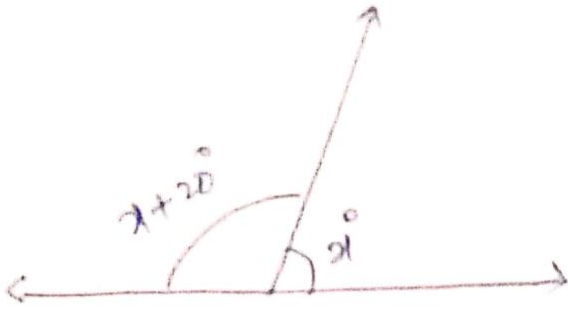


$$x + 130 = 180$$

$$x = 180 - 130$$

$$= 50^\circ$$

b)



$$x + 20^\circ + x = 180^\circ$$

$$2x + 20^\circ = 180^\circ$$

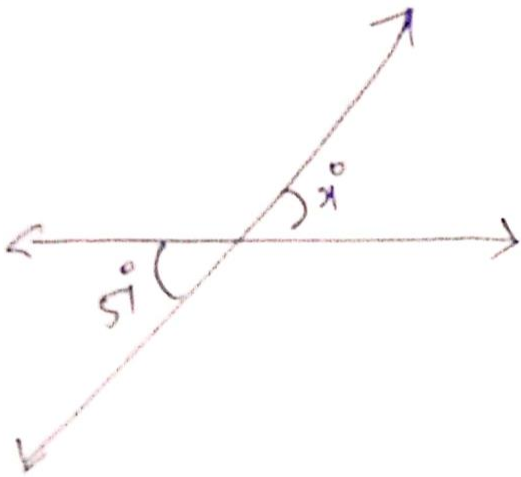
$$2x = 180^\circ - 20^\circ = 160^\circ$$

$$2x = 160$$

$$x = \frac{160^\circ}{2} = 80^\circ$$

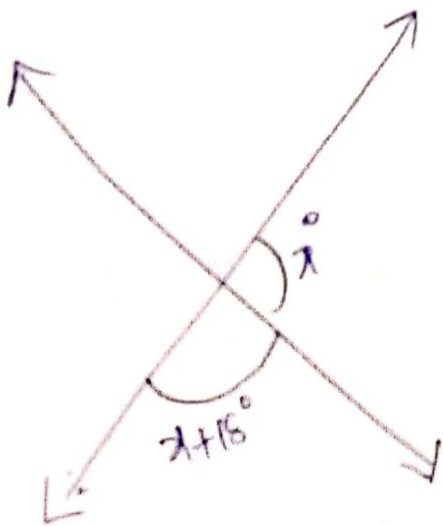
$$x + 20^\circ$$

c)



$$x = 51^\circ \text{ (opposite angles are equal)}$$

d)



$$x + 18^\circ + x = 180^\circ \text{ (adj. angles)}$$

$$2x + 18^\circ = 180^\circ$$

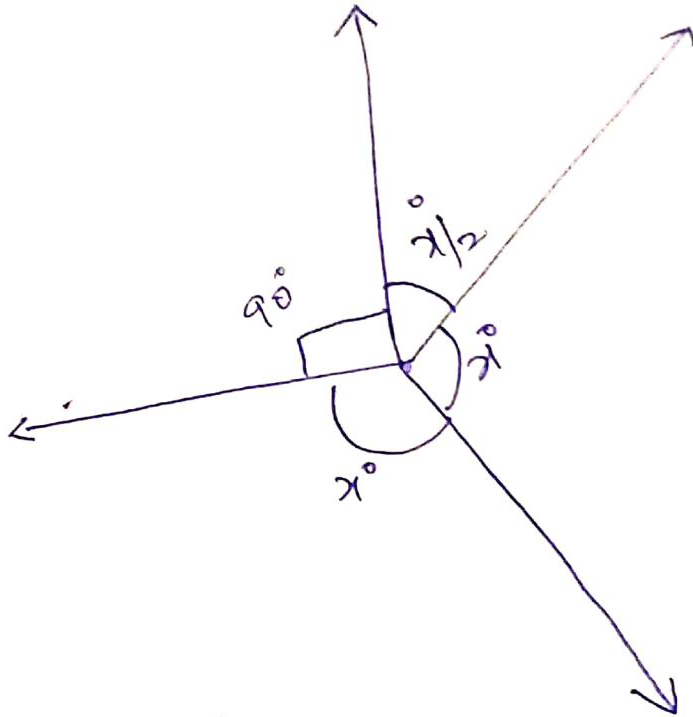
$$2x = 180^\circ - 18^\circ$$

$$= 162^\circ$$

$$x = \frac{162^\circ}{2} = 81^\circ$$

$$x = 81^\circ$$

6



$$x^\circ + x^\circ + \frac{x^\circ}{2} + 90^\circ = 360^\circ$$

$$2x^\circ + \frac{x^\circ}{2} + 90^\circ = 360^\circ$$

$$\frac{4x + x}{2} + 90 = 360$$

$$\frac{5x}{2} = 360 - 90$$

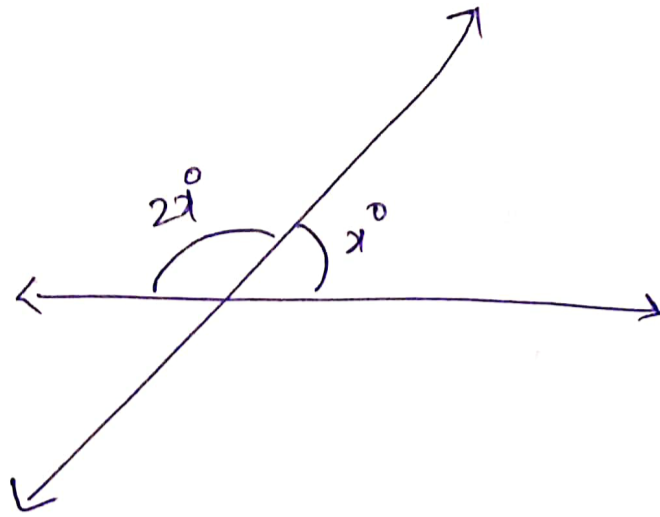
$$\frac{5x}{2} = 270$$

$$5x = 270 \times 2 = 540$$

$$5x = 540^\circ$$

$$x = \frac{540^\circ}{5} = 108^\circ$$

f)



Q

$$2x^\circ + x^\circ = 180^\circ \quad (\text{Linear pair})$$

$$3x = 180^\circ$$

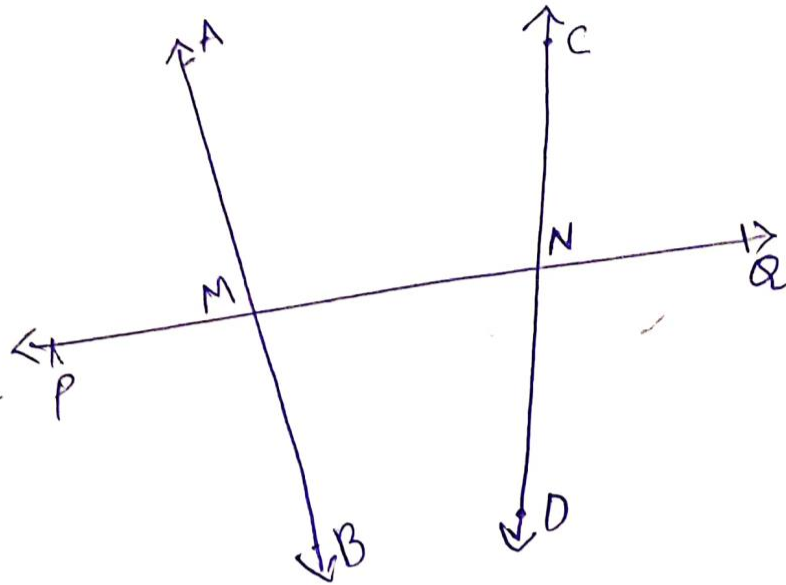
$$x = \frac{180^\circ}{3}$$

$$x = 60^\circ$$

(5)

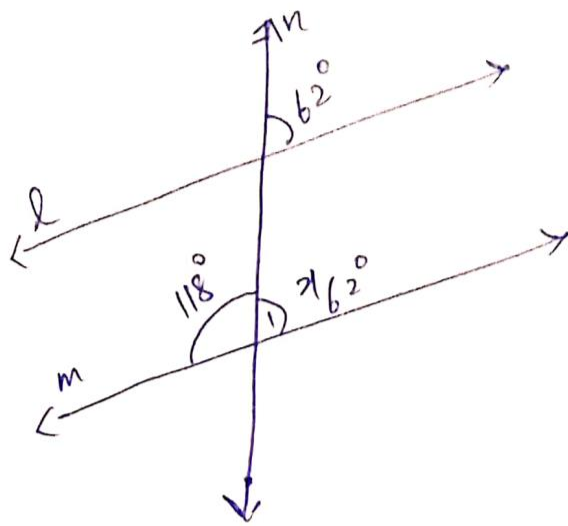
Exercise 10.2

1. Name the required angles in figure shown below



- a) The angle vertically opposite to $\angle AMN = \angle BMP$
- b) The angle alternate to $\angle CNQ = \angle BMP$
- c) The angle alternate to $\angle MNC = \angle QND$
- d) The angle corresponding to $\angle BMP = \angle CNQ$
- e) The angle corresponding to $\angle BMN = \angle CNM$
- f) The angle vertically opposite to $\angle QND = \angle CNM$
- g) The angle alternate to $\angle MND = \angle BMN$
- (k) The angle alternate to $\angle AMP = \angle CNQ$
- (i) The angle vertically opposite to $\angle PMB = \angle AMN$
- (j) The angle corresponding to $\angle CNQ = \angle BMP$

2. Lines l and m are intersected by transversal n . The measures of two angles are given in the figure is $l \parallel m$? Give reasons for your answer.



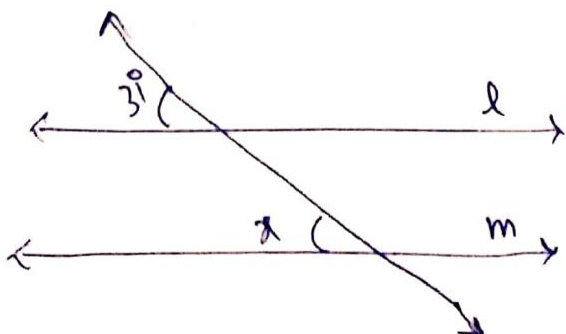
$$118^\circ + x = 180^\circ \quad \because$$

$$x = 180 - 118^\circ$$

$$= 62^\circ$$

If the corresponding angles are equal, then two lines l and m are parallel to each other.

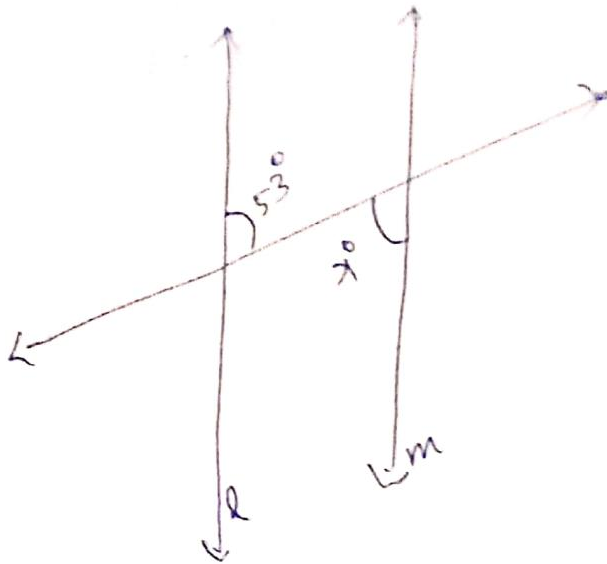
3. Given $l \parallel m$. Find the measure of x in the following figures.



$$x = 31^\circ$$

(R)

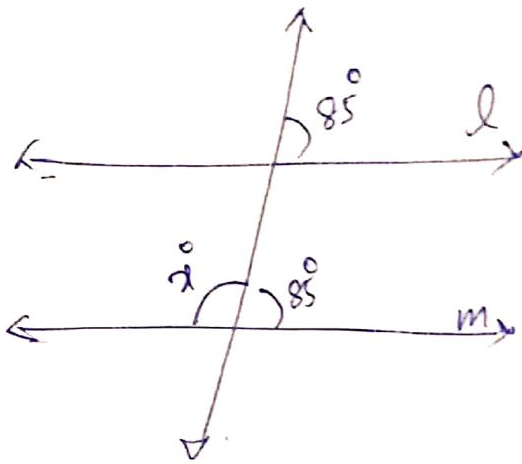
b)



$$x = 53^\circ$$

alternate interior angles are equal

c)



$$x^\circ + 85^\circ = 180^\circ$$

$$x = 180 - 85$$

$$= \underline{\underline{95^\circ}}$$

4. Given $l \parallel m$ and $\angle 1 = 71^\circ$, find the measures of all the other angles in the figure below.

$$\angle 1 = 71^\circ$$

$$\angle 1 + \angle 4 = 180$$

$$\angle 4 = 180 - \angle 1$$

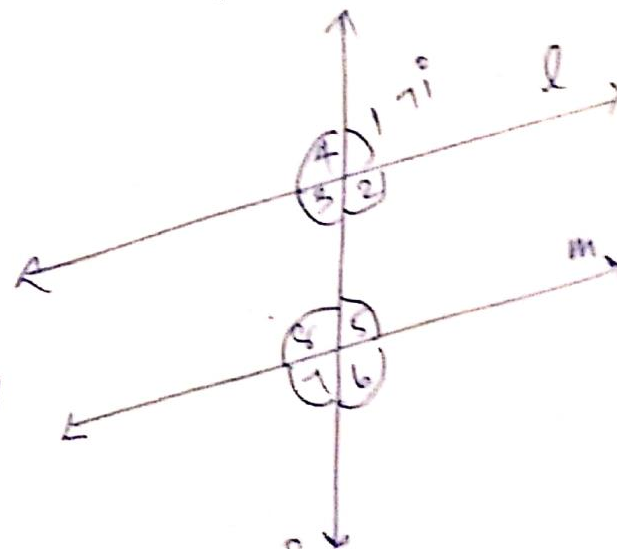
$$= 180 - 71 = \underline{\underline{109^\circ}}$$

$$\angle 1 = \angle 3 \text{ (opposite angles are equal)}$$

$$\angle 4 = \angle 2 = 109^\circ$$

$$\angle 5 = \angle 1 = \text{alternate angles.}$$

$$= 71^\circ$$



$$\angle 8 = \angle 4 = 109^\circ$$

$$\angle 8 = \angle 6 = 109^\circ$$

5. Given $l \parallel m$. Find the measures of $\angle 1$ and $\angle 2$ in the figure shown below

$$x^\circ + 3x^\circ + 4 = 180^\circ$$

$$4x^\circ + 4 = 180^\circ$$

$$4x = 180 - 4$$

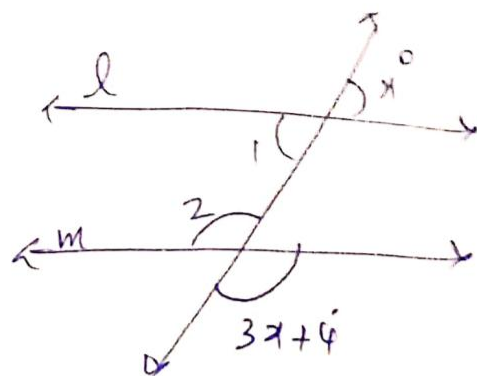
$$4x = 176$$

$$\frac{x = 176^\circ}{4} = \frac{44^\circ}{1}$$

$$x = \angle 1 = 44^\circ$$

$$\angle 2 = 3x + 4 = 3 \times 44 + 4$$

$$= ~~176~~ 132 + 4 = \underline{136^\circ}$$



Chapter. Check up

1). Find the complements of the following angles

a) $45^\circ = 90 - 45 = 45^\circ$

(f) $25^\circ = 90 - 25 = 65^\circ$

b) $8^\circ = 90 - 8 = 82^\circ$

(g) $78^\circ = 90 - 78 = 12^\circ$

c) $20^\circ = 90 - 20 = 70^\circ$

(h) $43^\circ = 90 - 43 = 47^\circ$

d) $85^\circ = 90 - 85 = 5^\circ$

(i) $18^\circ = 90 - 18 = 72^\circ$

e) $13^\circ = 90 - 13 = 77^\circ$

j) $4^\circ = 90 - 4 = 86^\circ$

2. Find the Supplements of the following angles

a) $50^\circ = 180^\circ - 50^\circ = 130^\circ$

b) $150^\circ = 180^\circ - 150^\circ = 30^\circ$

c) $105^\circ = 180^\circ - 105^\circ = 75^\circ$

d) $73^\circ = 180^\circ - 73^\circ = 107^\circ$

e) $128^\circ = 180^\circ - 128^\circ = 52^\circ$

(f) $140^\circ = 180 - 140 = 40$

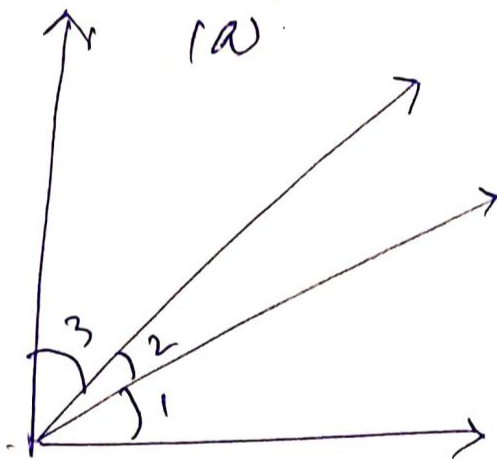
(g) $169^\circ = 180 - 169 = 11$

(h) $100^\circ = 180 - 100 = 80$

(i) $106^\circ = 180 - 106 = 74$

(j) $29^\circ = 180 - 29 = 151$

3. Identify the pairs of adjacent angles in the following figures.

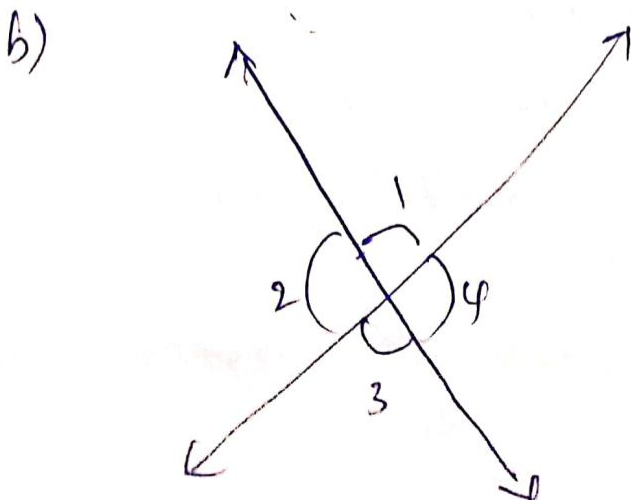


$$\angle 1 = \angle 2$$

$$\angle 2 = \angle 3$$

$$\angle 1 + \angle 2 = \angle 3$$

$$\angle 3 + \angle 2 = \angle 1$$



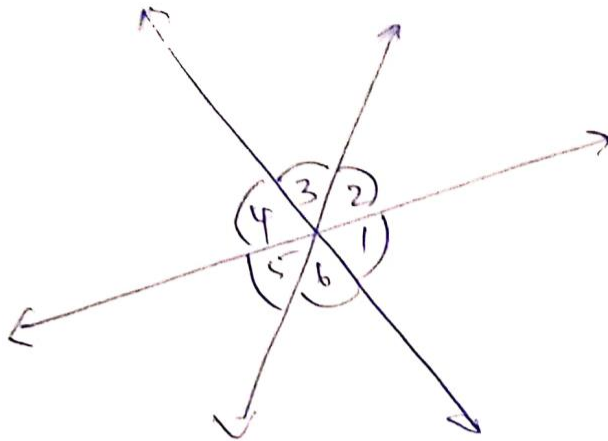
$$\angle 1 = \angle 4$$

$$\angle 1 = \angle 2$$

$$\angle 2 = \angle 3$$

$$\angle 4 = \angle 3$$

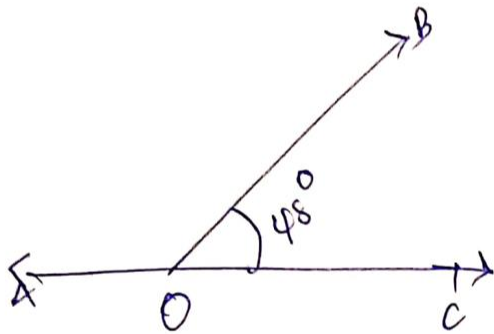
c)



$$\begin{aligned} \angle 1 &= \angle 6 \\ \angle 1 &= \angle 2 \\ \angle 3 &= \angle 2 \\ \angle 3 &= \angle 4 \\ \angle 4 &= \angle 5 \\ \angle 5 &= \angle 6 \\ \angle 6 &= \angle 1 \end{aligned}$$

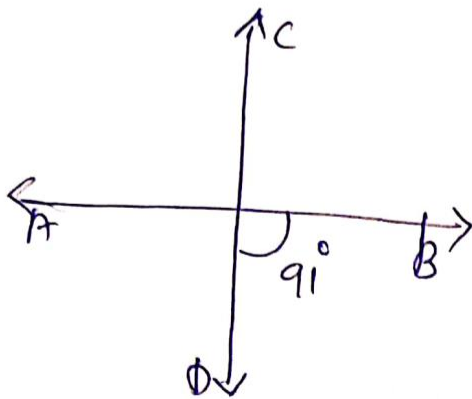
4. Find all the angles in the following figures.

a)



$$\begin{aligned} \angle AOB + \angle BOC &= 180^\circ \\ \angle AOB &= 180^\circ - \angle BOC \\ &= 180^\circ - 48^\circ \\ \angle AOB &= \underline{\underline{132^\circ}} \end{aligned}$$

b)



$$\angle AOD + \angle BOD = 180^\circ$$

$$\begin{aligned} \angle AOD &= 180 - \angle BOD \\ &= 180 - 91^\circ = 89^\circ \end{aligned}$$

$$\angle BOD = \angle AOC = 91^\circ \text{ (opposite angles)}$$

$$\angle BOD = 91^\circ$$

$$\angle AOD = \angle BOC = 89^\circ$$

c)

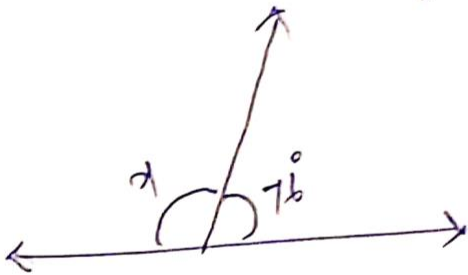


$$\begin{aligned} \angle AOD + \angle BOD &= 180^\circ \\ \angle BOD &= 180 - 33^\circ \\ &= \underline{\underline{147^\circ}} \end{aligned}$$

$$\begin{aligned} \angle AOC &= \angle BOD = 147^\circ \\ \angle AOD &= \angle BOC = \underline{\underline{33^\circ}} \end{aligned}$$

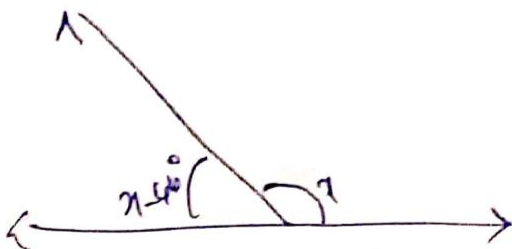
5. Find the value of x in the following figures.

a)



$$\begin{aligned} x + 76^\circ &= 180 \\ x &= 180 - 76^\circ \\ &= \underline{\underline{104^\circ}} \end{aligned}$$

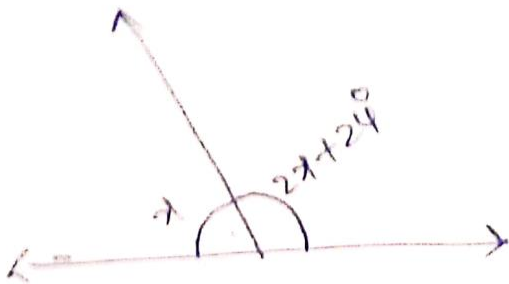
b)



$$\begin{aligned} x - 44 + x &= 180 \\ 2x - 44 &= 180 \\ 2x &= 180 + 44 = 224 \\ x &= \frac{224}{2} = \underline{\underline{112^\circ}} \\ x - 44 &= 112^\circ - 44 \\ &= \underline{\underline{68^\circ}} \end{aligned}$$

$\frac{112}{68}$

c)



$$x + 2x + 24^\circ = 180$$

$$3x + 24^\circ = 180^\circ$$

$$3x = 180 - 24^\circ = 156^\circ$$

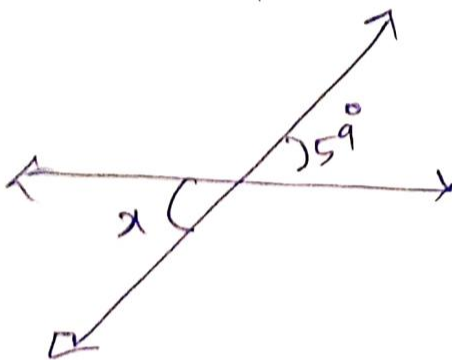
$$x = \frac{156^\circ}{3} = \underline{\underline{52^\circ}}$$

$$2x + 24 = 2(52) + 24$$

$$= 104 + 24$$

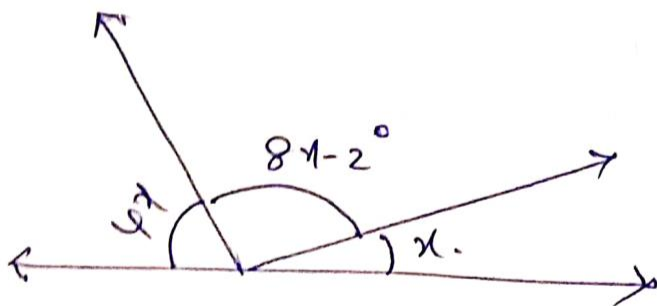
$$= \underline{\underline{128^\circ}}$$

d)



$$x = 59^\circ$$

e)



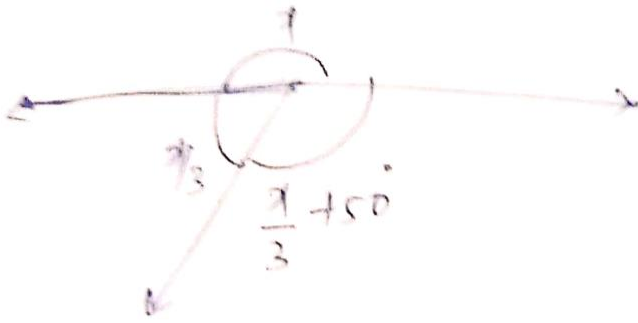
$$4x + 8x - 2^\circ + x = 180^\circ$$

$$4x + 8x + x - 2 = 180$$

$$13x = 180 + 2$$

$$x = \frac{182^\circ}{13} = \underline{\underline{14^\circ}}$$

f)



$$x + \frac{x}{3} + \frac{x}{3} + 50 = 360^\circ$$

$$x + \frac{2x}{3} + 50 = 360$$

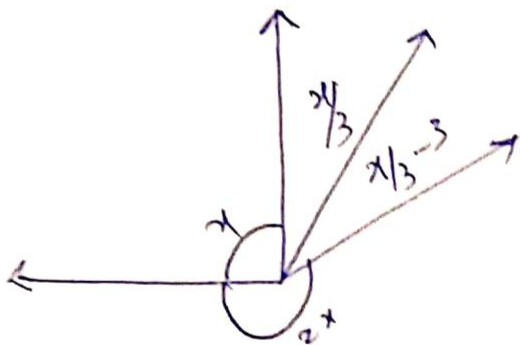
$$\frac{3x + 2x}{3} = 360 - 50 = 310$$

$$\frac{5x}{3} = 310$$

$$5x = 310 \times 3 = 930$$

$$x = \frac{930}{5} = \underline{\underline{186^\circ}}$$

g)



$$x + \frac{x}{3} + \frac{x}{3} - 3 + 2x = 360^\circ$$

$$3x + \frac{2x}{3} = 360 + 3^\circ$$

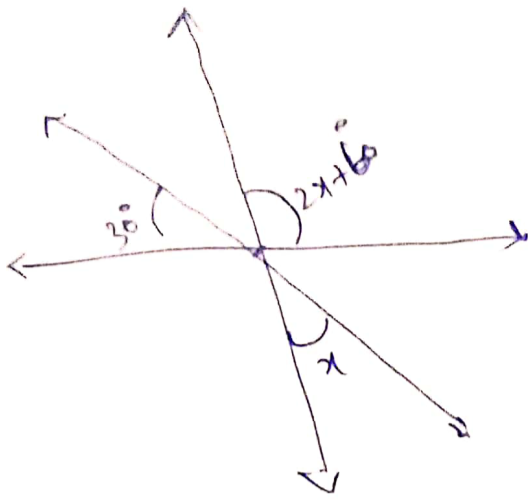
$$\frac{9x + 2x}{3} = 363^\circ$$

$$\frac{11x}{3} = 363$$

$$11x = 363 \times 3 = 1089$$

$$x = \frac{1089}{11} = \underline{\underline{99^\circ}}$$

h)



$$30 + x + 2x + 6 = 180^\circ$$

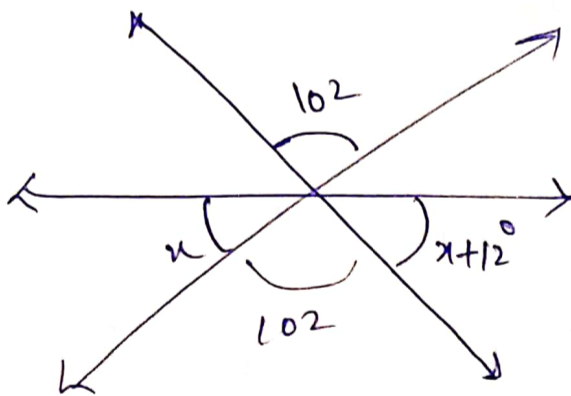
$$3x + 36 = 180$$

$$3x = 180 - 36$$

$$3x = 144$$

$$x = \frac{144}{3} = \underline{\underline{48^\circ}}$$

i)



$$x + 102^\circ + x + 12^\circ = 180^\circ$$

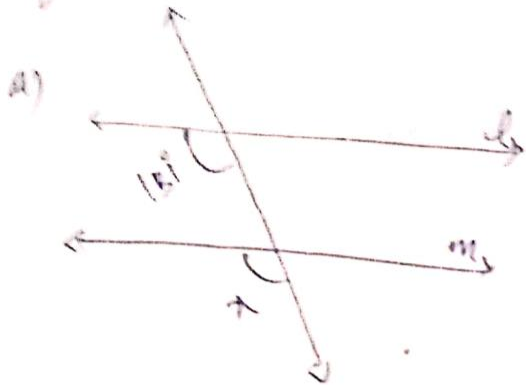
$$2x + 114^\circ = 180^\circ$$

$$2x = 180 - 114$$

$$2x = 66^\circ$$

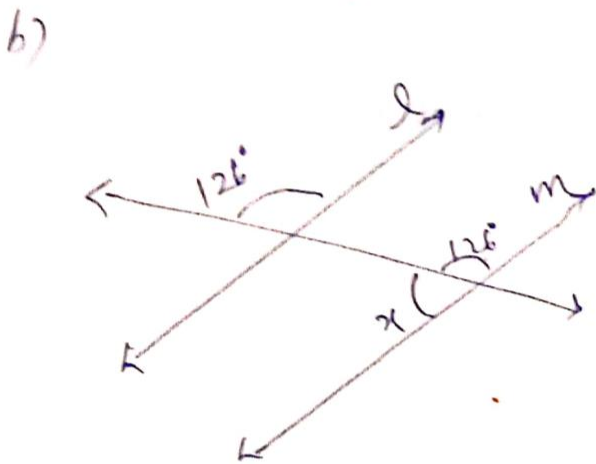
$$x = \frac{66^\circ}{2} = \underline{\underline{33^\circ}}$$

6. Given lines or rays $l \parallel m$ in the following figures, find the measure of x .



Corresponding angles are equal $l \parallel m$.

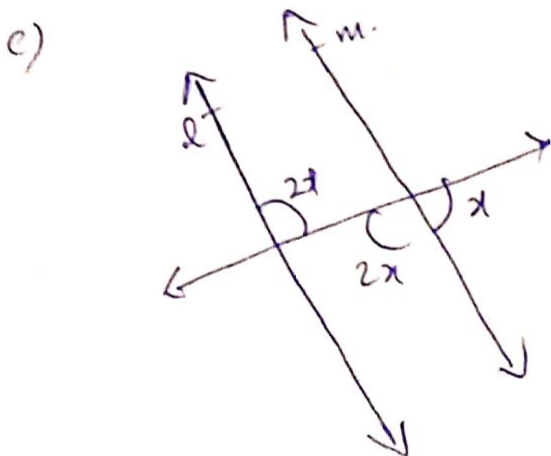
$$\underline{\underline{x = 131^\circ}}$$



$$x + 126^\circ = 180$$

$$x = 180 - 126^\circ$$

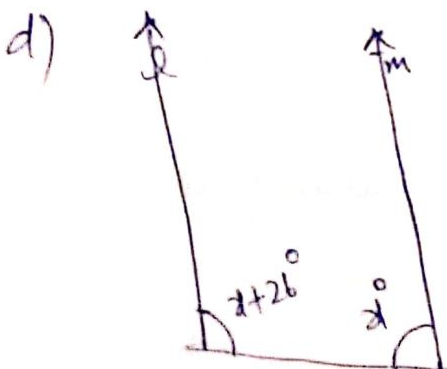
$$= \underline{\underline{54^\circ}}$$



$$x + 2x = 180^\circ$$

$$3x = 180^\circ$$

$$x = \frac{180}{3} = 60^\circ$$

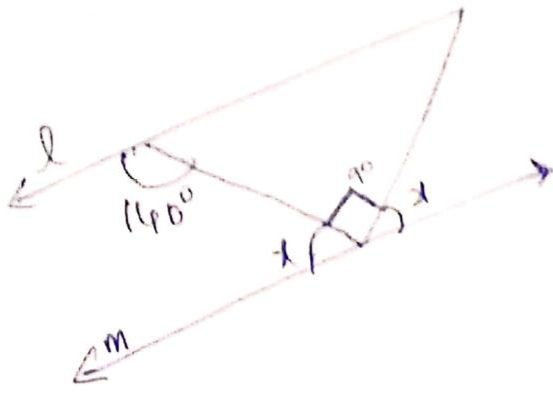


$$x + 26 + x = 180^\circ$$

$$2x + 26 = 180$$

$$2x = 180 - 26 = \underline{\underline{154}}$$

$$x = \frac{154}{2} = \underline{\underline{77^\circ}}$$

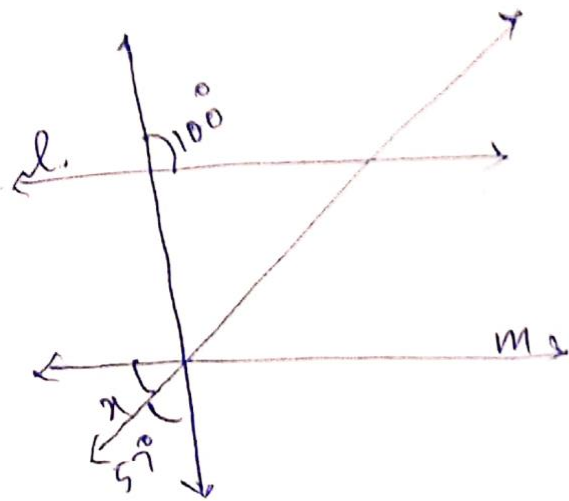


$$x + 90 + 140 = 180$$

$$2x = 180 - 90 = 90$$

$$x = \frac{90}{2} = 45$$

f)



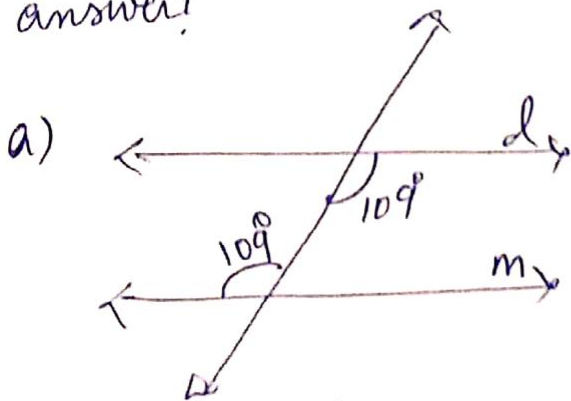
alternate exterior angles are equal

$$x + 57 = 100$$

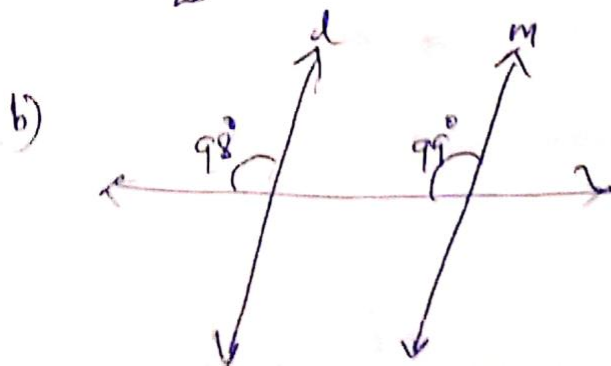
$$x = 100 - 57$$

$$= \underline{\underline{43}}$$

a) Are lines l & m parallel to each other in the following figures? Give reasons for your answer?

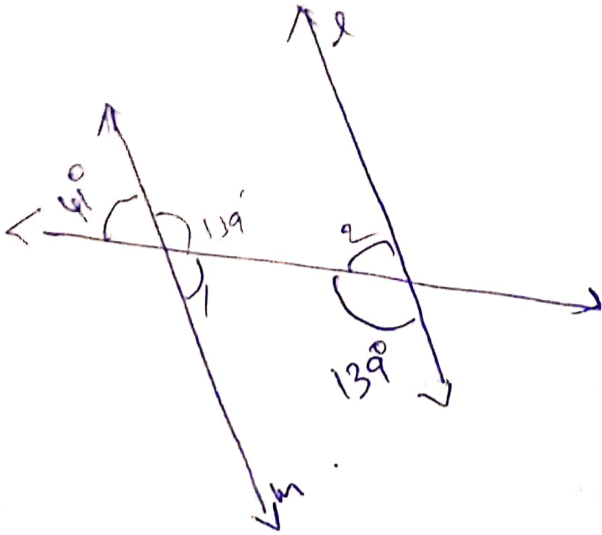


$l \parallel m$ (alternate interior angles are equal)



l not parallel to m
 $l \not\parallel m$ corresponding angles are not equal so lines l and m intersect each other

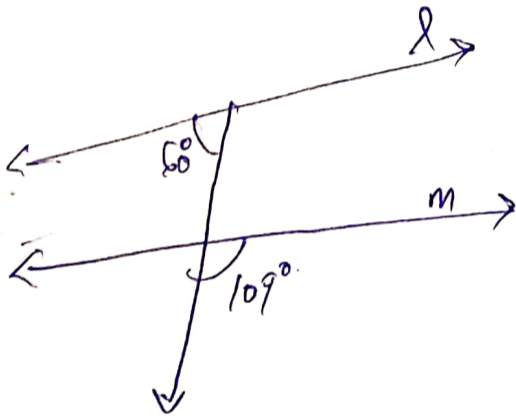
c)



l and m are parallel
alternate interior angles are
equal

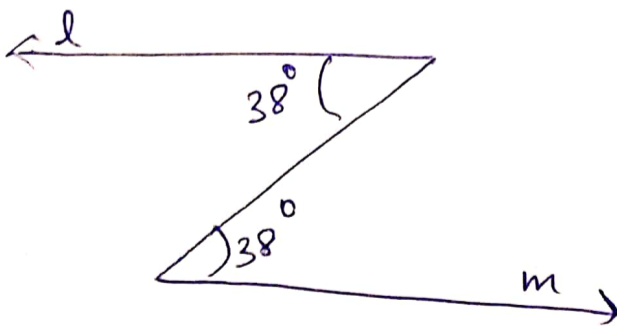


d)

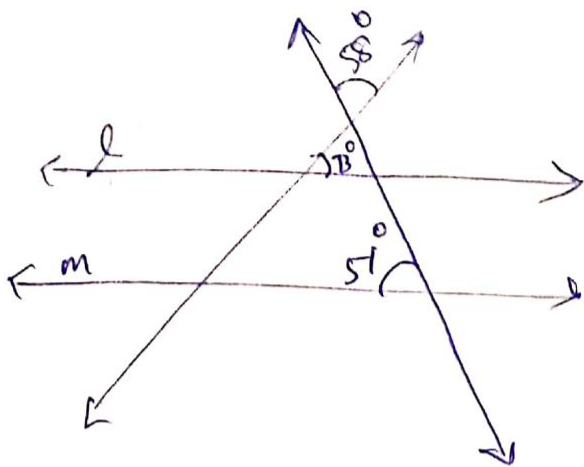


l and m are not parallel
Corresponding and alternate
Angles are not equal
~~The~~ lines l and m intersect
each other

e)



alternate interior angles
are equal then
 $l \parallel m$.

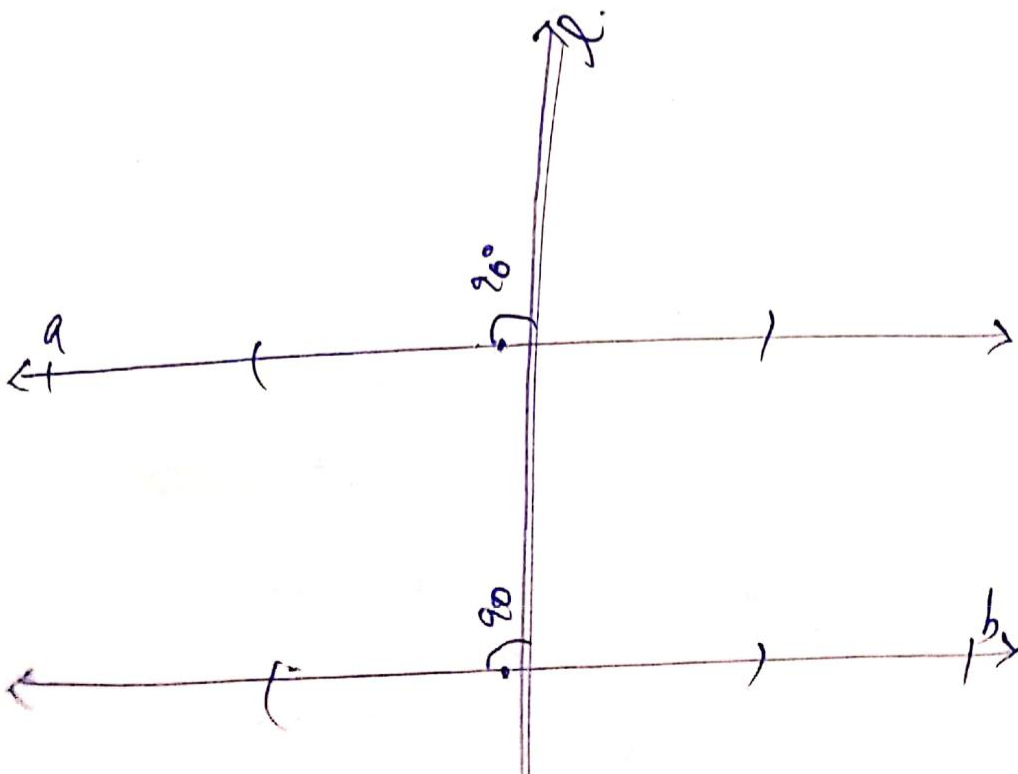


$$\begin{array}{r}
 180 - \\
 (73) \\
 \hline
 107 \\
 180 - \\
 131 \\
 \hline
 49
 \end{array}$$

$$73 + 51 + 58$$

l & m not parallel
 (interior angles are not equal.)

the transversal l is perpendicular to line a
 well as line b is $a \parallel b$? construct a diagram
 illustrate your answer!



1. Mark the probability of the following in the line
- (a) Probability of a cat giving birth to a dog: $P(C)$
 - (b) The Sun will rise on Monday: $P(M)$
 - (c) The chance that red will show up when a spinner with colours (red, blue, yellow and green) is rotated.
 - (d) The chance that a girl is chosen from a group of 6 girls and 6 boys: $P(G)$

Solution

(a) A cat will never give birth to a dog. So its probability is zero. i.e. $P(C) = 0$

(b) The Sun will rise on Monday. There are 7 days in a week. In that we have 1 chance for rise of Sun on Monday. So its probability is $\frac{1}{7}$. i.e. $P(M) = \frac{1}{7}$

(c) Number of colours in the spinner = 4
In that possibility to get red = 1
 \therefore Its probability $P(R) = \frac{1}{4}$

(d) Number of persons in the group = 12

2. Six friends were deciding where to go

The coming weekend. Everyone wrote their choice on a slip of paper to show their choices.

Fishing, Boating, Waterpark, Cricket match, Cricket match, Hillside

Write the probability of the following

(a) $P(\text{waterpark}) = ?$

Total number of choices = 6

No. of waterpark option = 1

$\therefore P(\text{waterpark}) = \frac{1}{6}$

(b) $P(\text{cricket match}) = ?$

Total number of choices = 6

No. of cricket match option = 2

$\therefore P(\text{cricket match}) = \frac{2}{6} = \frac{1}{3}$

(c) $P(\text{fishing}) = ?$

Total number of choices = 6

No. of fishing option = 1

$P(\text{fishing}) = \frac{1}{6}$

(d) $P(\text{cinema}) = ?$

3. The letters of the word "PROBABILITY" are put in a bag and one letter is taken out.

(i) There are _____ Outcomes.

(ii) What is the Probability of the following being the

(a) $P(P) = \underline{\quad}$ (b) $P(R) = \underline{\quad}$ (c) $P(B) = \underline{\quad}$

(d) $P(L) = \underline{\quad}$ (e) $P(\text{Vowels}) = \underline{\quad}$ (f) $P(\text{Consonants}) = \underline{\quad}$

(g) $P(X) = \underline{\quad}$ (h) $P(\text{any letter}) = \underline{\quad}$

Solution:

(i) The letters are 'P', 'R', 'O', 'B', 'A', 'I', 'L', 'I', 'T', 'Y'.

Number of letters = 9.

\therefore There are 9 Outcomes.

(ii) (a) $P(P) = ?$

No. of 'P' in the bag = 1

$\therefore P(P) = \underline{\underline{\frac{1}{9}}}$

(b) $P(R) = ?$

No. of 'R' in the bag = 1

$\therefore P(R) = \underline{\underline{\frac{1}{9}}}$

(c) $P(B) = ?$

No. of 'B' in the bag = 2

$\therefore P(B) = \underline{\underline{\frac{2}{9}}}$

(e) $P(\text{Vowels}) = ?$

No. of Vowels = 4

$\therefore P(\text{Vowels}) = \frac{4}{9}$

(f) $P(\text{Consonants}) = ?$

No. of Consonants = 5

$P(\text{Consonants}) = \frac{5}{9}$

(g) $P(x) = ?$

No. of 'x' in bag = 0

$\therefore P(x) = 0$

(h) $P(\text{any letter}) = ?$

No. of 'letters' in bag = 9

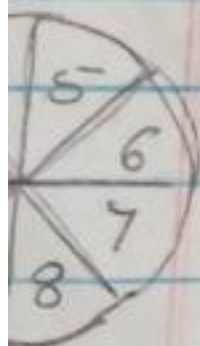
$P(\text{any letter}) = \frac{9}{9} = 1$

4. Here is an Octagonal Spinner 1, 2, 3, 4 are marked on it. Write the probabilities of Occurrence of the following events.

(a) Spinner lands on 4, $P(4) = \frac{1}{8}$

(b) Spinner lands on an even number,
 $P(\text{even}) = ?$

No. of even numbers = 4



(c) Spinner lands on ten, $P(10) =$ _____

There is no 10 in the Spinner

$$\therefore \underline{\underline{P(10) = 0}}$$

(d) Spinner lands on a number less than 4,

$$P(\text{less than } 4) =$$

No: less than 4 on Spinner = 3

$$P(\text{less than } 4) = \frac{3}{9} = \underline{\underline{\frac{1}{3}}}$$

(e) $P(\text{less than } 9) = ?$

No: of less than 9 on Spinner = 8

$$P(\text{less than } 9) = \underline{\underline{\frac{8}{9}}}$$

(f) $P(3 \text{ to } 6) = ?$

No: of from 3 to 6 on Spinner = 4

$$P(3 \text{ to } 6) = \underline{\underline{\frac{4}{9}}}$$

Chapter check up ∴

1. Draw a Scale from 0 to 1 for each of events. Mark the Scale to show the probability of each event.

(a) Renu is tossing a coin. what is the probability of it landing on tails?

either a head or a tail. So total n
of chances = 2

In that probability of getting a tail = $\frac{1}{2}$

(b) There are 10 beads in a bag. Only one
bead is red. what is the chance of picking
red bead?

Soln: Total beads in a bag = 10

In that No. of red beads = 1

\therefore Probability (red bead) = $\frac{1}{10}$

~~(c) what is the chance of sun rising at mid~~

(c) what is the chance of sun rising at mid
tonight?

Soln:- Sun will not rise in midnight. So probability will
be zero.

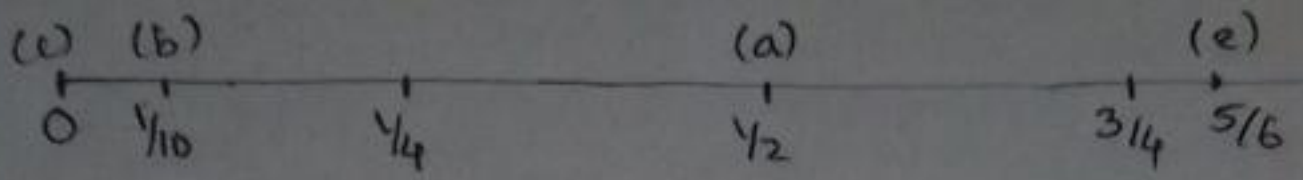
(d) Asif is holding a brick. what is the proba
that when he lets go of it, the brick will drop

Soln:- When he drops the brick, it will ~~drop~~

So the probability will be 1

(e) Naaz closes her eyes. what is the chance

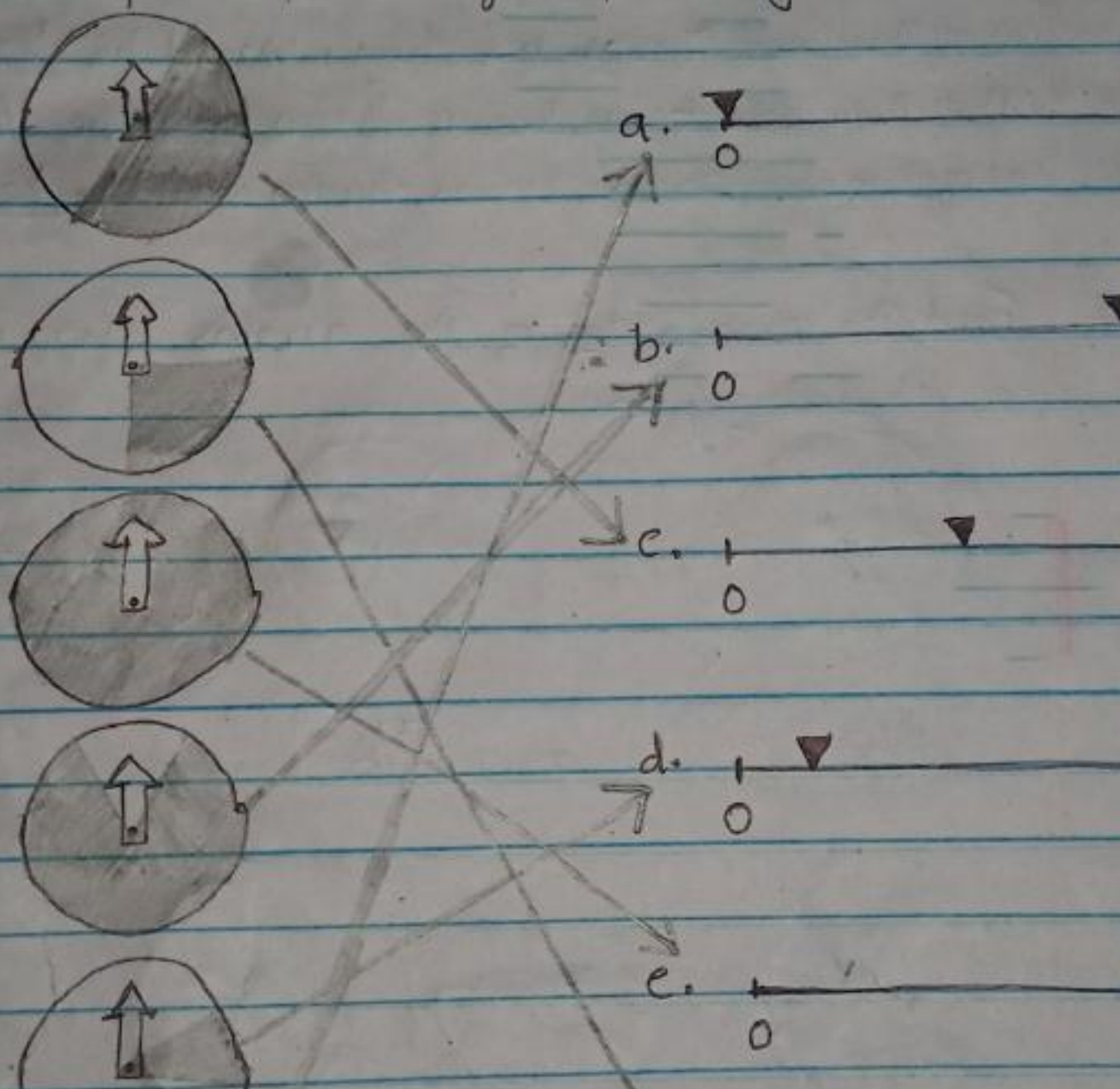
that she will pick a white cube from the



Soln:- There are 6 cubes. In that there are 5 white cubes.

\therefore probability (white cubes) = 5/6

2. To win, The arrow of the Spinner must 'land' on shaded part. Match the probability of winning using each spinner with one of the probability Scales shown.



3. Fill in The blanks.

Karan goes to a funfair and plays. Find
Marble. There are 3 cups. A marble is hidden
under one of them.

(a) Karan's chances of picking the cup with
marble under it are $\frac{1}{3}$

(b) If there are 5 cups, his chance would be $\frac{1}{5}$

(c) If there were 7 cups, his chance would be $\frac{1}{7}$

(d) If there were 4 cups, Karan's chances would be $\frac{1}{4}$

(e) If there were 20 cups, Karan's chances would be $\frac{1}{20}$

4. Find The probability of The arrows stopping
a shaded region



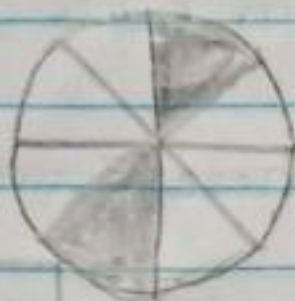
$\frac{2}{8}$



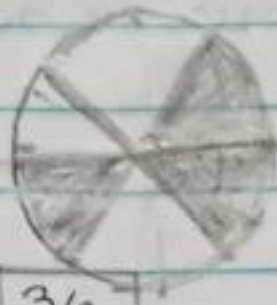
$\frac{3}{6}$



5. Find The probability of the arrow stopping on white Section in each drawing above. Give your answer as fractions.



$$\frac{6}{8}$$



$$\frac{3}{6}$$



$$\frac{2}{4}$$



$$\frac{6}{10}$$



$$\frac{4}{8}$$



$$\frac{2}{6}$$

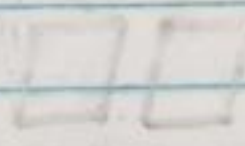


$$\frac{2}{4}$$

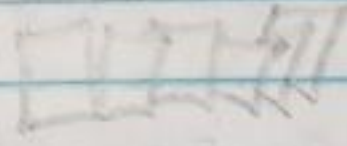
6. There are two red cards in each set given in the
 what is the probability of picking a red card?



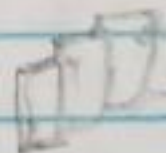
$$\frac{2}{5}$$



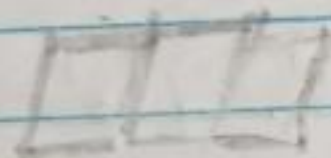
$$\frac{2}{2} = 1$$



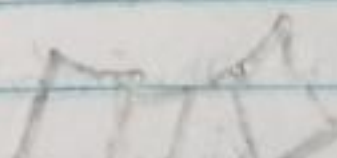
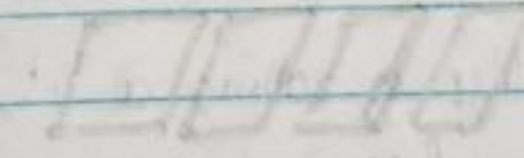
$$\frac{2}{6} = \frac{1}{3}$$



$$\frac{2}{8}$$



$$\frac{2}{3}$$



$$\frac{2}{4} = \frac{1}{2}$$

7. Out of The Sets given above, which is The from which you are certain to pick two cards on The first go?

Soln :- (b) There are only two cards.

8. Work out The chance of making These Scores a dice.

(a) The probability of rolling a 'six'?

Numbers in a dice = 1, 2, 3, 4, 5, 6

So total = 6

\therefore Probability of rolling a '6' = $\frac{1}{6}$

(b) Probability of rolling a 'one'?

Numbers in a dice = 1, 2, 3, 4, 5, 6

\therefore Probability of rolling a '1' = $\frac{1}{6}$

(c) The probability of rolling a 'one' or 'six'?

Numbers in a dice = 1, 2, 3, 4, 5, 6

Probability of rolling '1' or '6' = $\frac{2}{6} =$

(d) The probability of rolling a '1', '6', or '3'?

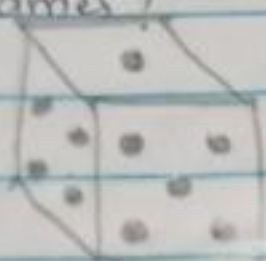
Numbers in a dice = 1, 2, 3, 4, 5, 6

(e) The probability of rolling a 'two', 'six', 'five', or 'three' on a die = $\frac{4}{6} = \frac{2}{3}$

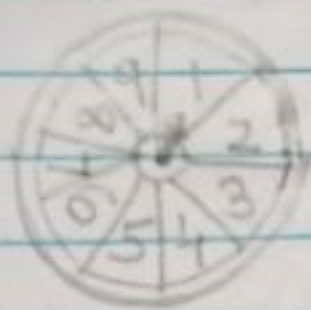
Number on dice = 1, 2, 3, 4, 5, 6

Probability of rolling '2', '6', '5', '3' = $\frac{4}{6} = \frac{2}{3}$

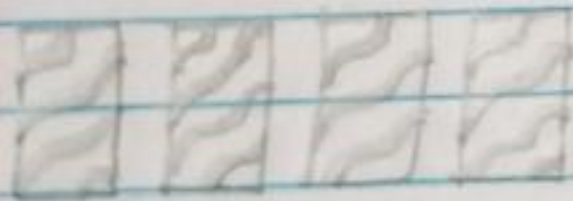
9. What are Rima's chances of winning in each of the games?



Rima's probability of picking the winning number is $\frac{1}{6}$



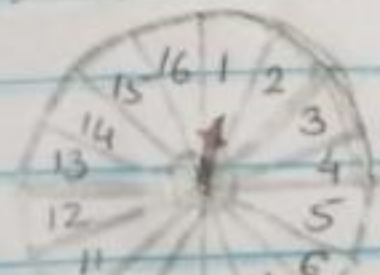
Rima's probability of picking the winning number is $\frac{1}{9}$



If there is only one ace, Rima's probability of picking the ace is $\frac{1}{4}$

19	7	22	6	11	32	10
37	17	2	29	3	8	16
4	28	5	18	14	33	25

If the shaded numbers are 1, 2, 3, 4, 5, 6, Rima's probability of picking the lucky number is $\frac{6}{36} = \frac{1}{6}$



Rima's probability of picking the winning number is $\frac{1}{16}$